

Electromagnetic inverse problems in biomedical engineering

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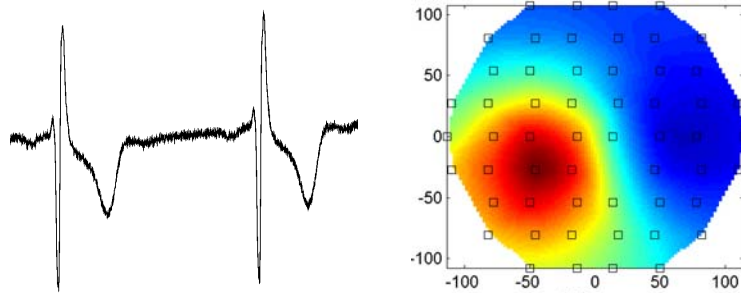
Biomagnetic Center, Department of Neurology, University Jena, Germany

Overview

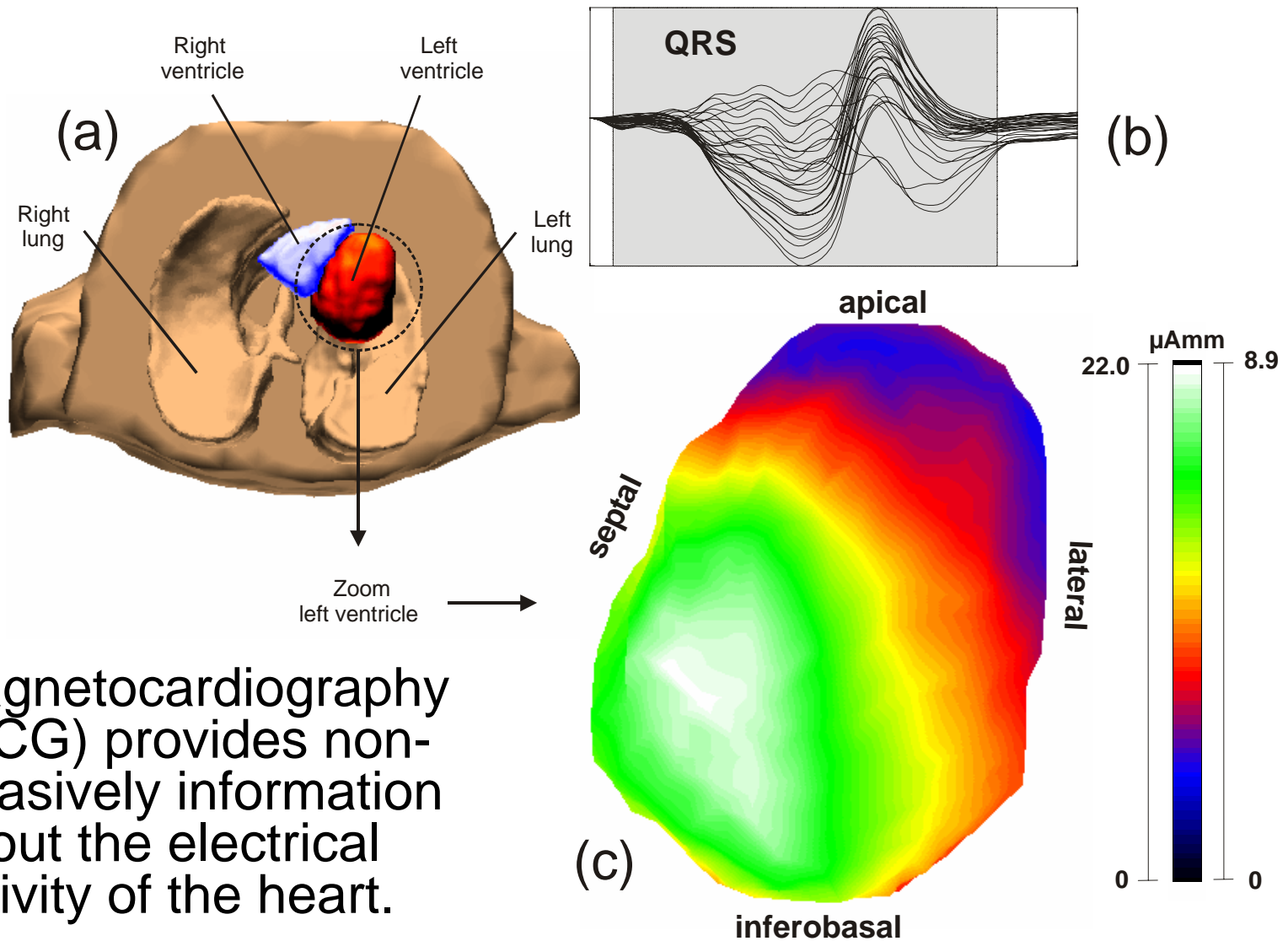
1. Introduction
2. Localization of magnetic markers in the alimentary tract
3. The influence of forward model conductivities on EEG/MEG source reconstruction
4. **Optimization of magnetic sensor arrays for magnetocardiography**
5. Validation of source reconstruction procedures

Magnetocardiography (MCG)

- Measurement of magnetic field produced by the heart
- Reconstruction of electric sources causing the field



MCG



Magnetocardiography (MCG) provides non-invasively information about the electrical activity of the heart.

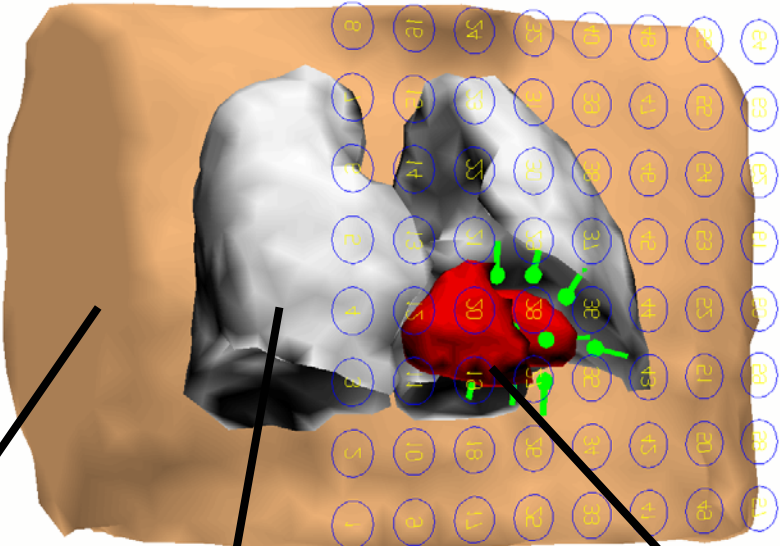
Introduction

- New room temperature optical magnetometers allow customized and flexible sensor arrangements
- Arising question: how do we arrange the sensors optimally?
- Goal function: condition number (CN) of the lead field (LF) matrix

BEM model



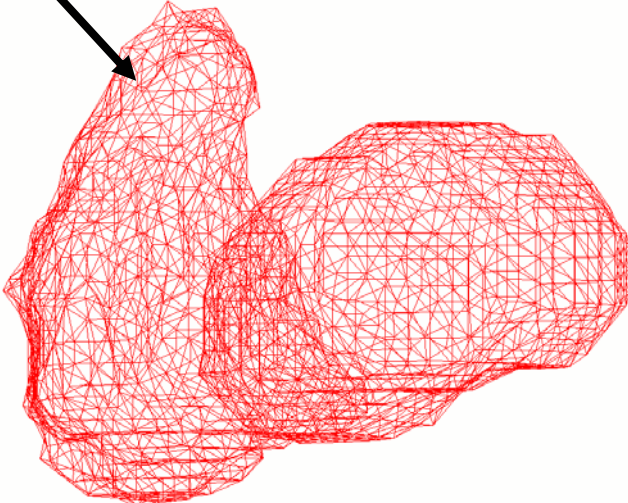
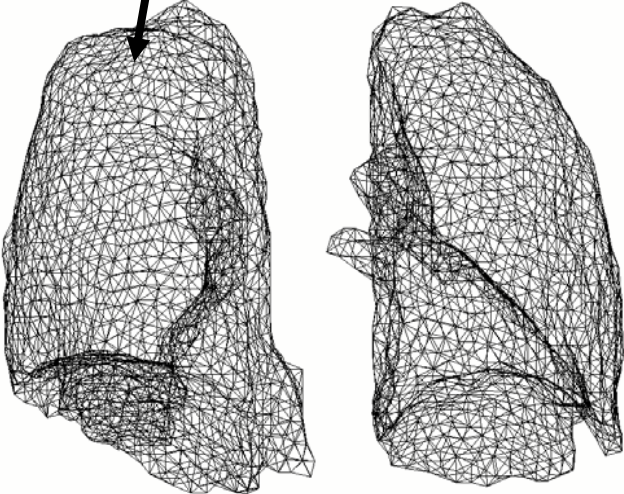
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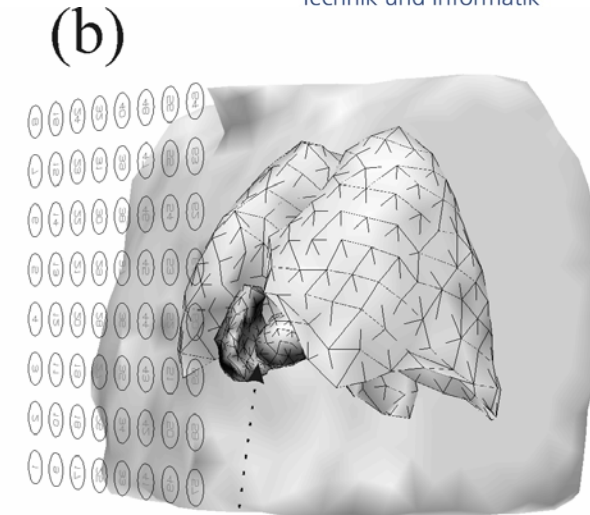
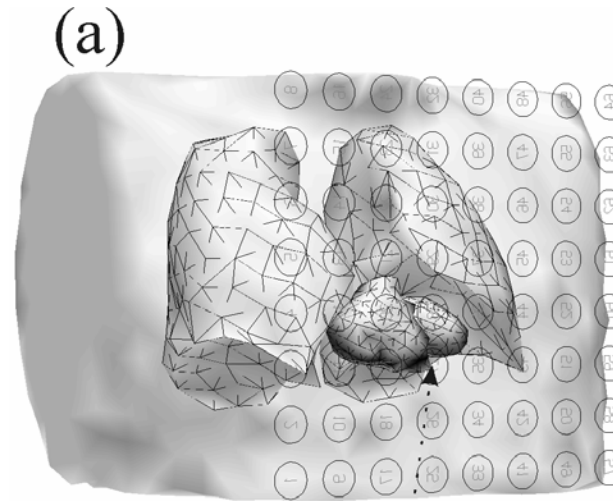
Torso

Lungs

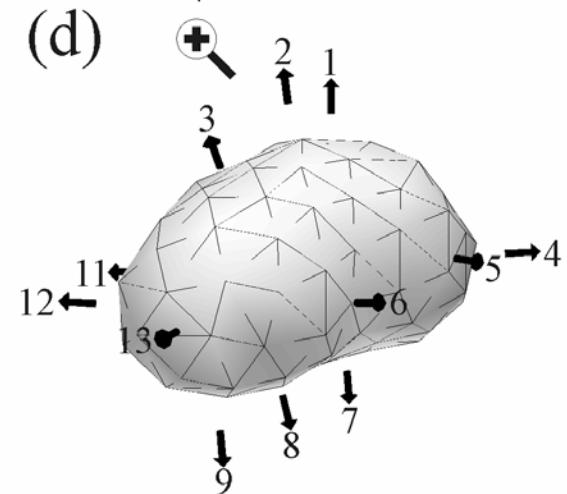
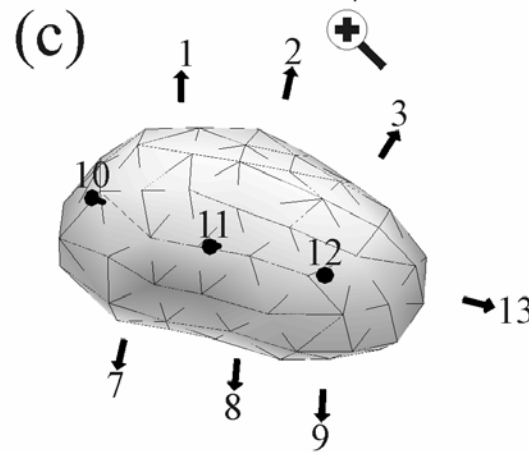
Ventricular
blood masses



Source space



13 current dipoles,
distributed around
the left ventricle
of the heart



The objective function

- LF matrix contains information on geometry of the source space, the boundary element model and the sensor array
- A minimal CN implies an optimal sensor arrangement for a given setup

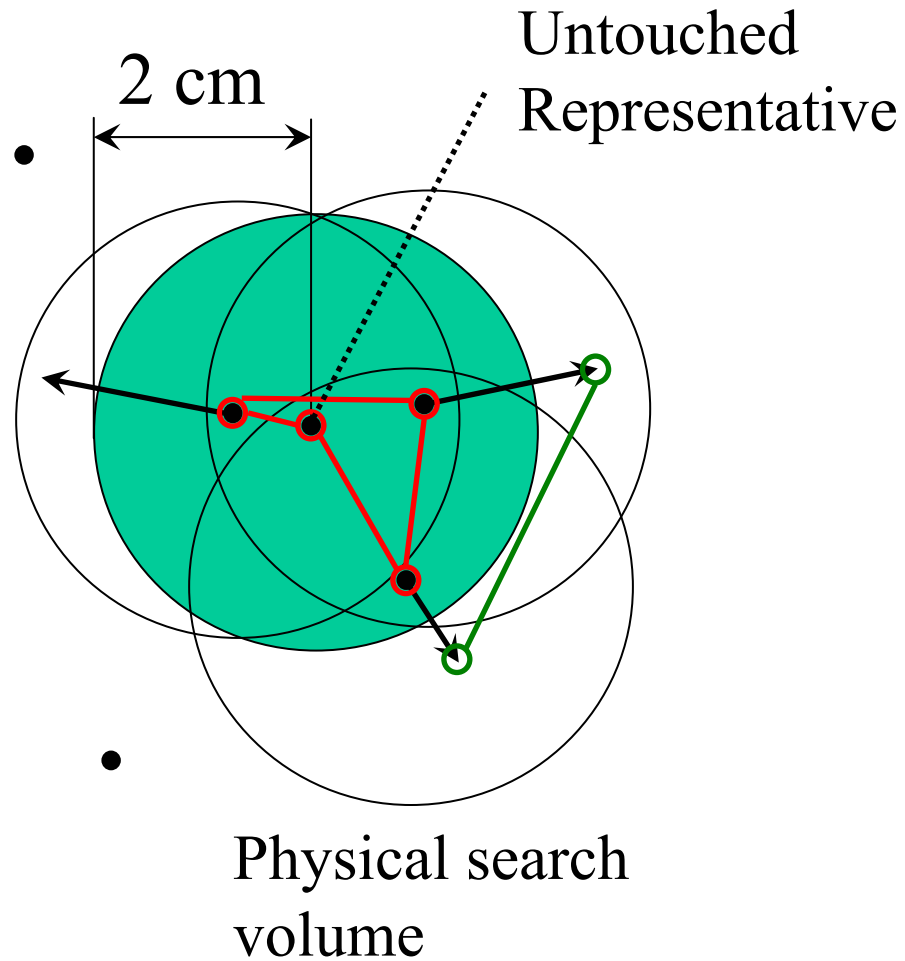
Discretization of the search space

- Optimization: iterative search for a sensor setup with minimal CN
- But LF computation is slow, therefore pre-computation for a fixed grid of positions & orientations is needed

Constraint Framework for Continuous Optimizers

- Discrete search volume
 - snap into grid before each CN evaluation
- Minimum distance (MD) of sensors, here 2 cm
 - while $\text{mean}(\text{MD violation}) > \text{tolerance}$
 1. pick a sensor with max #clashes
 2. move all clashing sensors away radially
 3. snap into grid
- Pro: one representative sensor out of the clashing sensors is kept

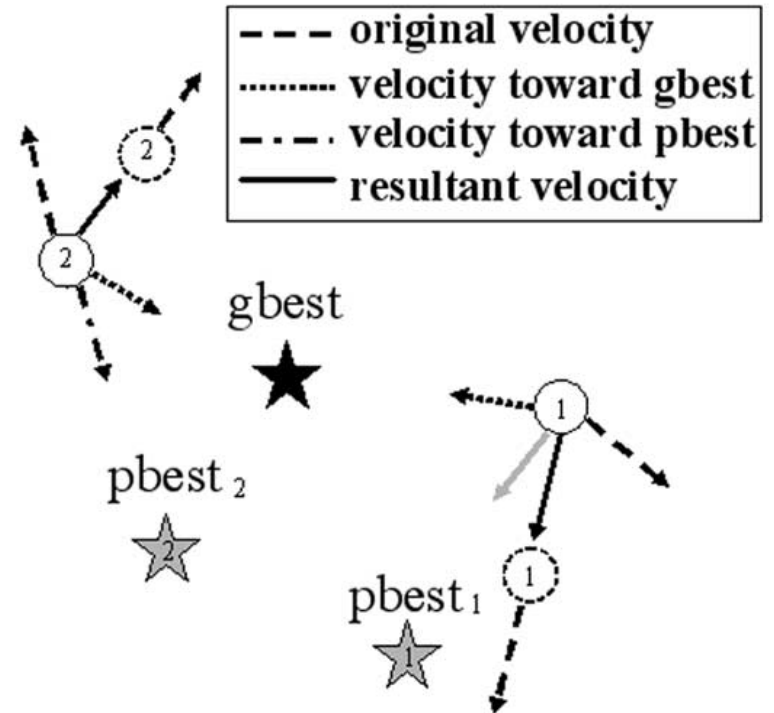
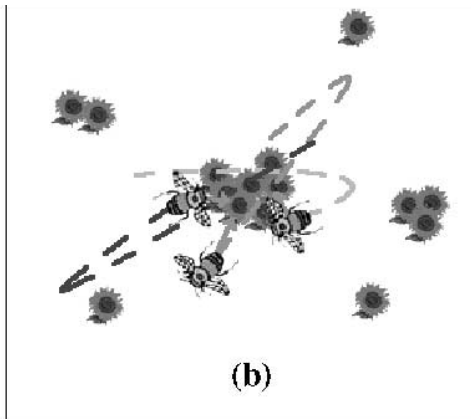
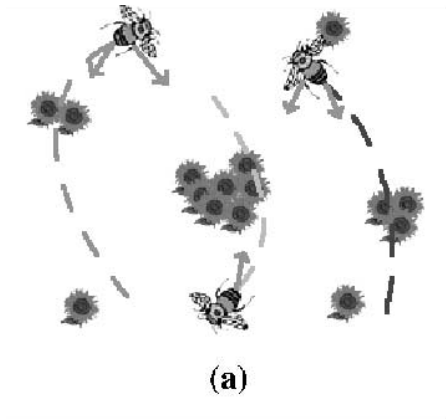
Restoring the minimum distance



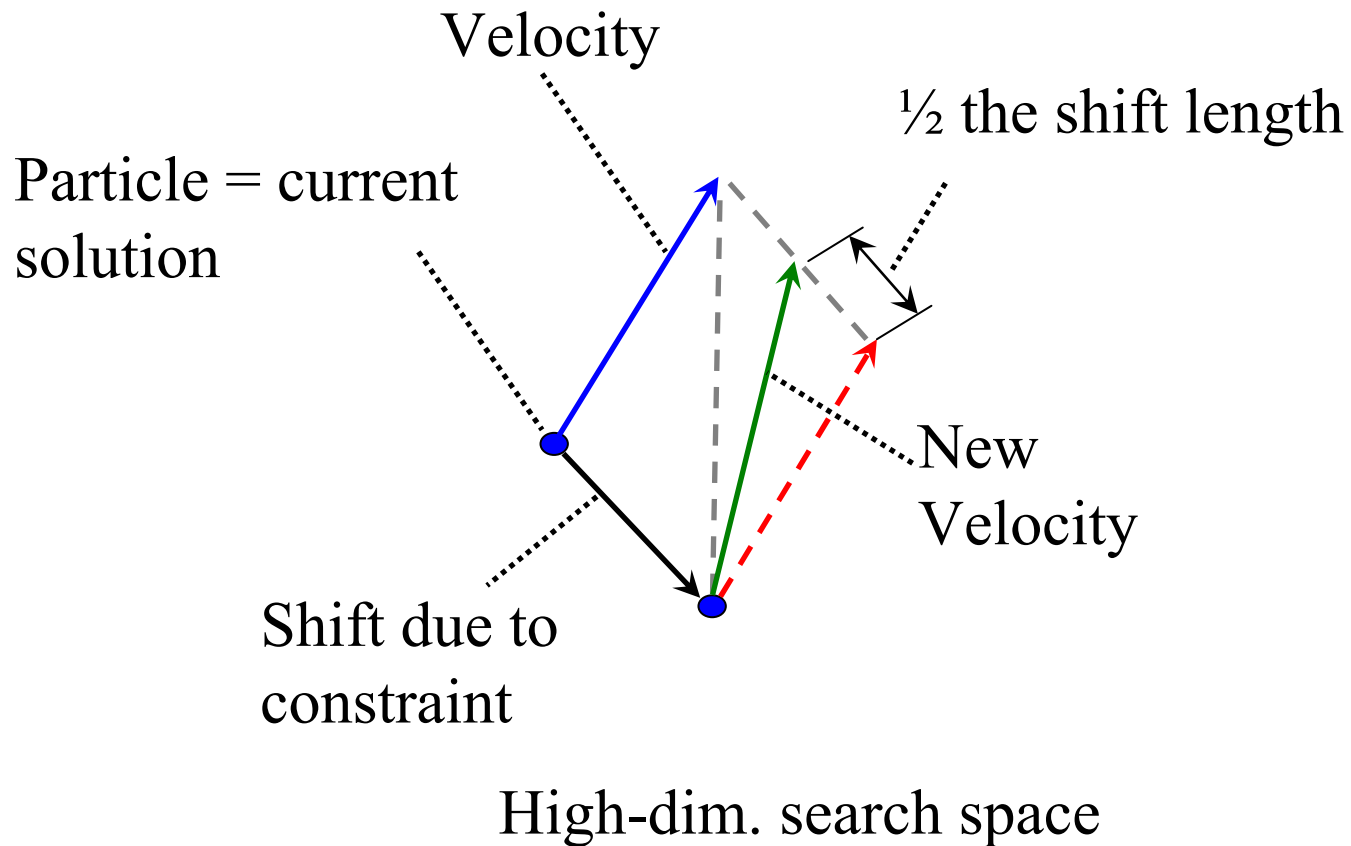
Particle Swarm Optimization (PSO)

- A set of candidate solutions (= particles) is randomly initialized
- Each particle has a position and velocity in high-dim. search space
- Each particle has informant particles, whose state it can access
- Iteration = move particles + update velocities + fix constraint
- After constraint fix, the velocities are corrected

PSO algorithm



PSO velocity correction



Tabu Search (TS)

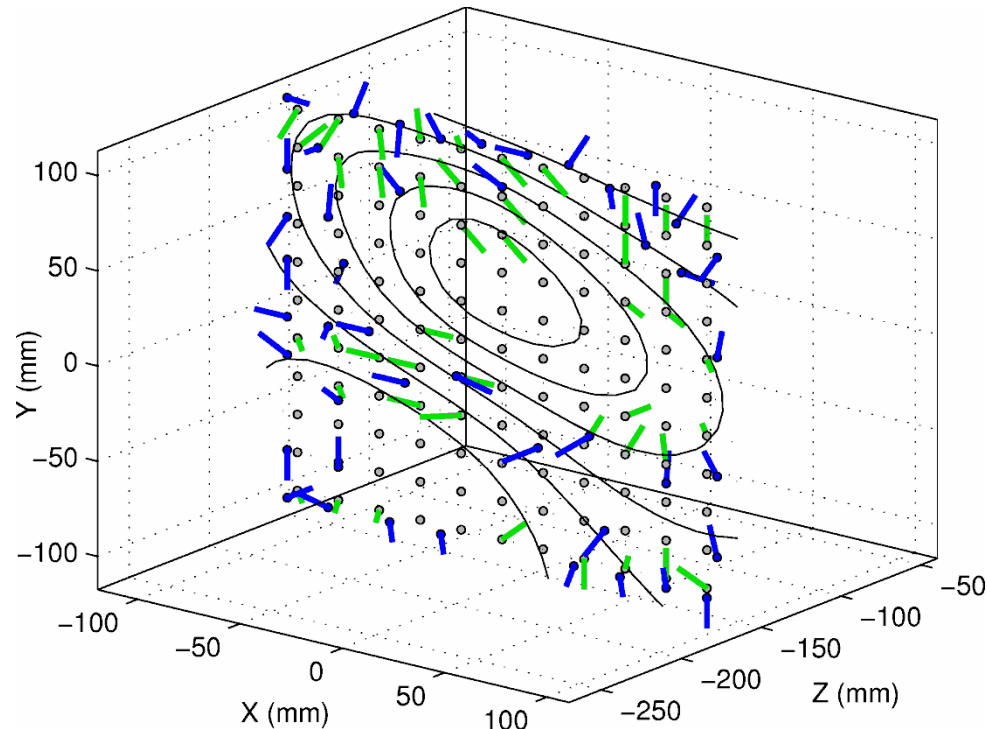
- Discrete search: combinatorial selection of s out of r sensors with minimal CN
- The minimum distance constraint is satisfied for all sensor selections
- In each iteration step: find a better selection of s sensors (with lower CN) in the neighborhood of the current solution by exchanging n sensors (during the search n was decreased from $s/2$ to 1)

PSO vs. TS

- TS prevents reevaluations of sensor configurations by memorizing them
- TS is robust against local minima
- But: no use of spatial closeness or gradient, limited to combinations of predefined sensor positions/orientations
- Dense grids (i.e. a higher number of sensors on the same area) may be more difficult to optimize than sparse ones because of the combinatorial complexity

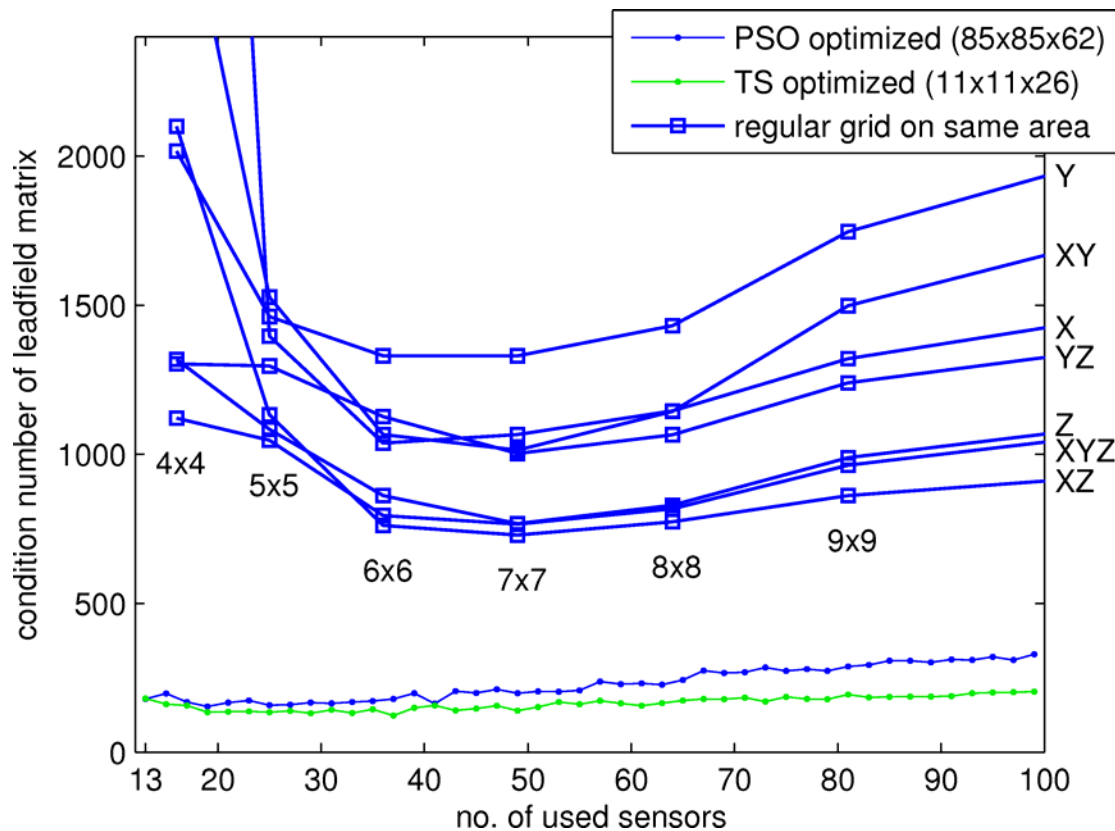
Numerical Results

- PSO and TS are implemented in C++ in SimBio: TS (green) and PSO (blue) optimized setups are very similar



Reduction of CN

- Both optimizations significantly reduce CN



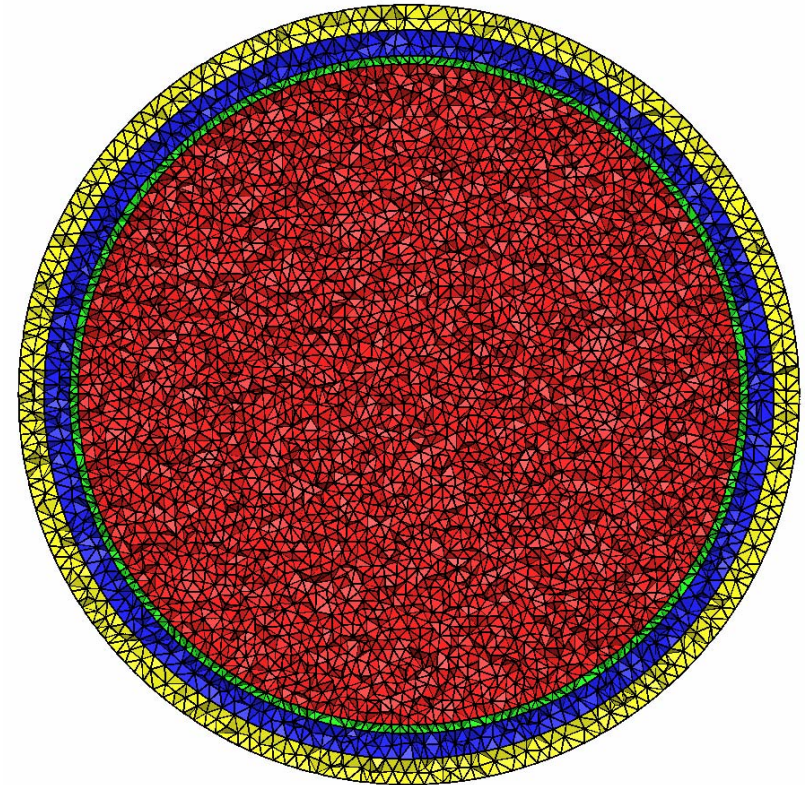
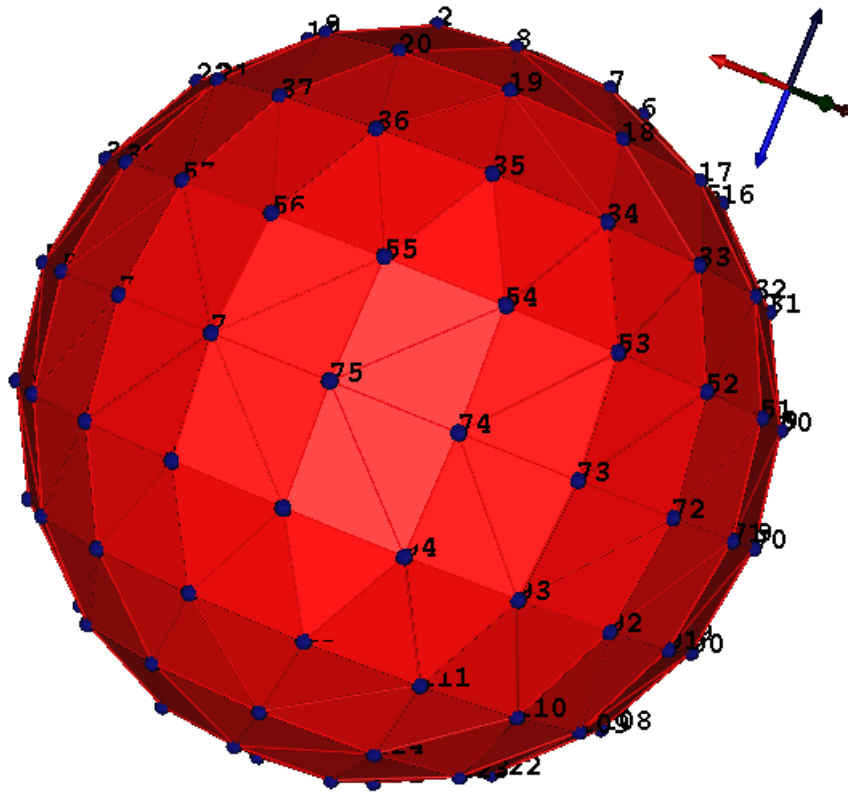
Conclusion

- Comparable results indicate that optimization of vectorial sensor setups may be significantly improved
- Reconstruction robustness may be improved and the number of sensors may be reduced while retaining information in terms of CN
- The new quasi-continuous PSO optimization incorporates the gradient and spatial closeness information while being robust against local minima in the goal function
- A fine 3D search volume, projection method based and lower error bound based sensor setup optimizations are planned

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- 5. Validation of source reconstruction procedures**
 1. Simulations
 2. Phantom measurements
 3. Animal measurements

Simulations



4-layer sphere model:

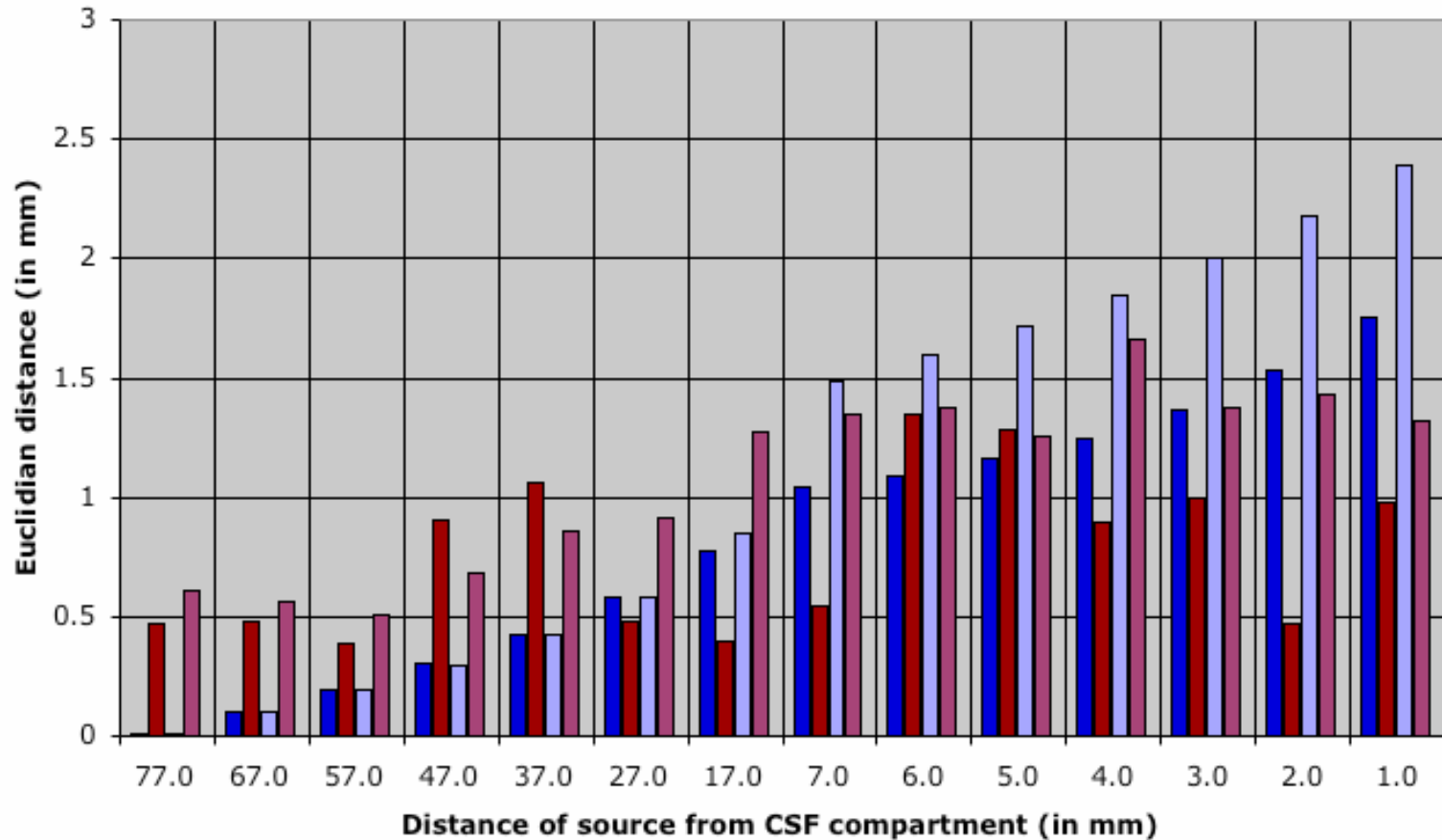
134 electrodes

**Radii: 92, 86, 80, 78mm;
0.33, 0.0042:0.042, 1.79, 0.33 S/m**

Nodes: 161,086

Simulations

Dipole localization error



Forward: J.C. de Munck

Inverse: FEM

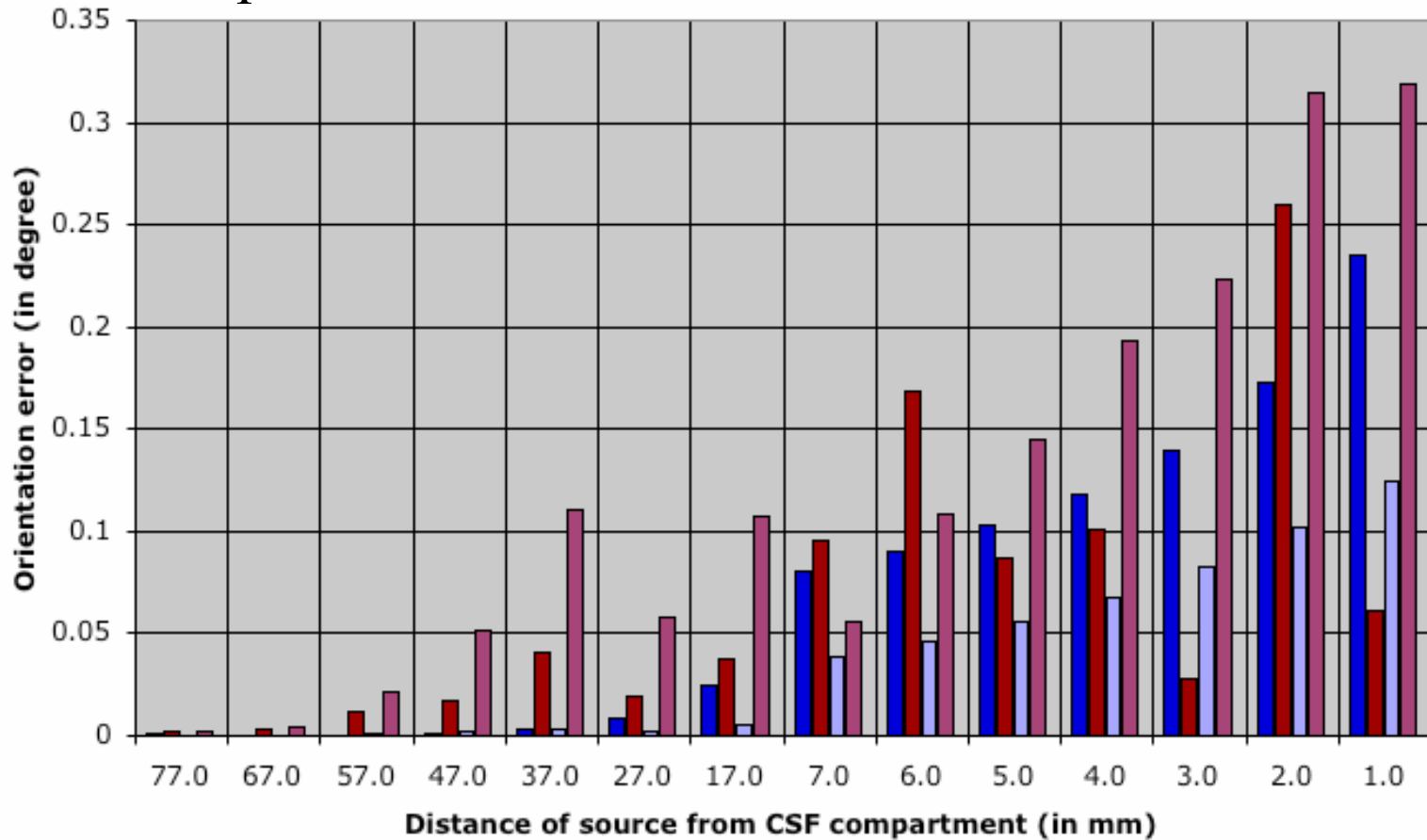


Simulations



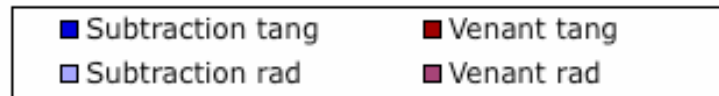
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Dipole orientation error



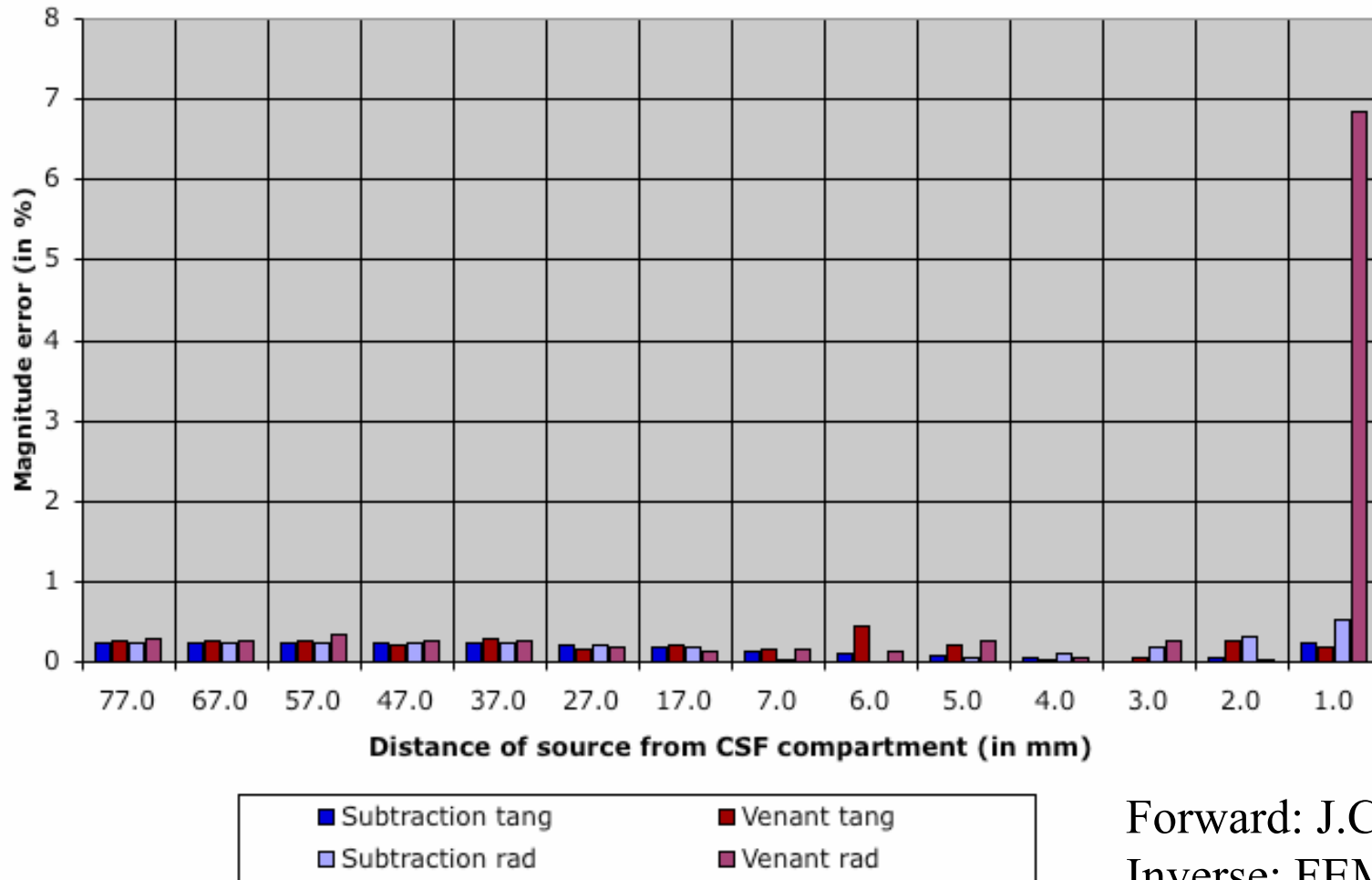
Forward: J.C. de Munck

Inverse: FEM



Simulations

Dipole magnitude error

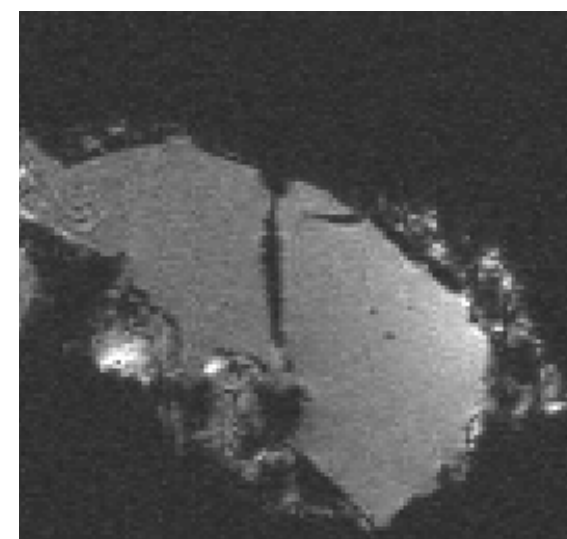
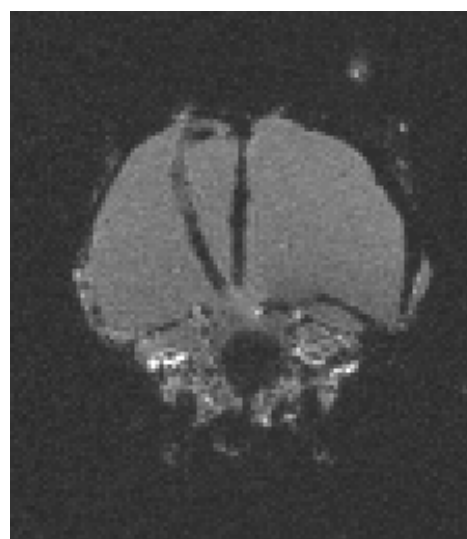
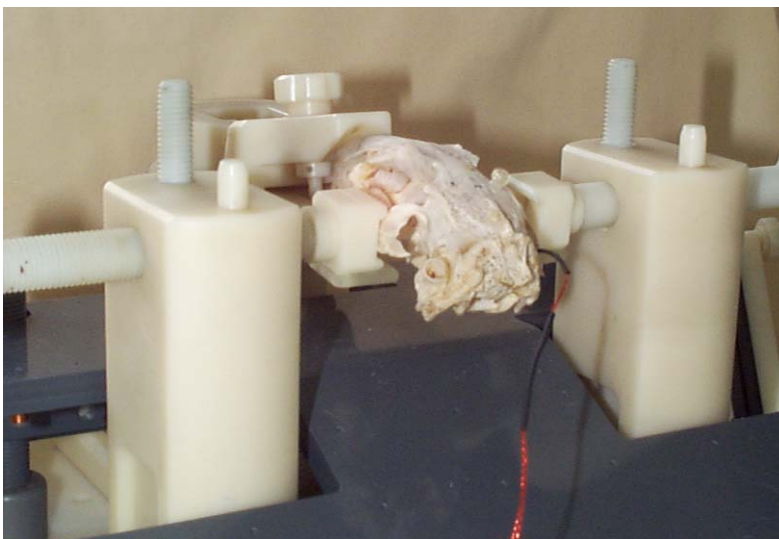
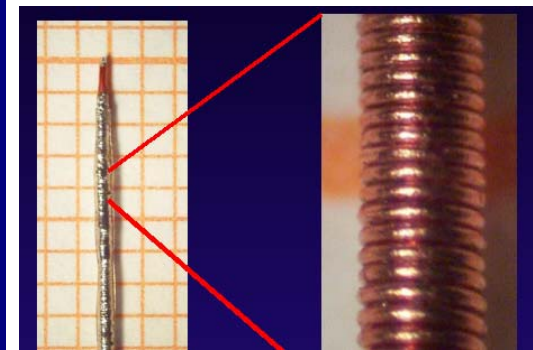
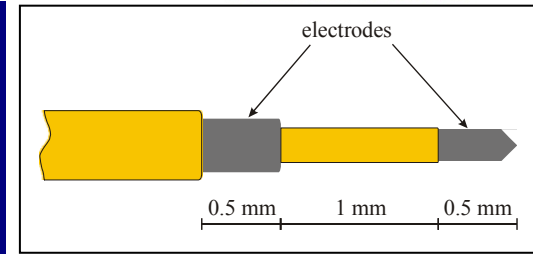
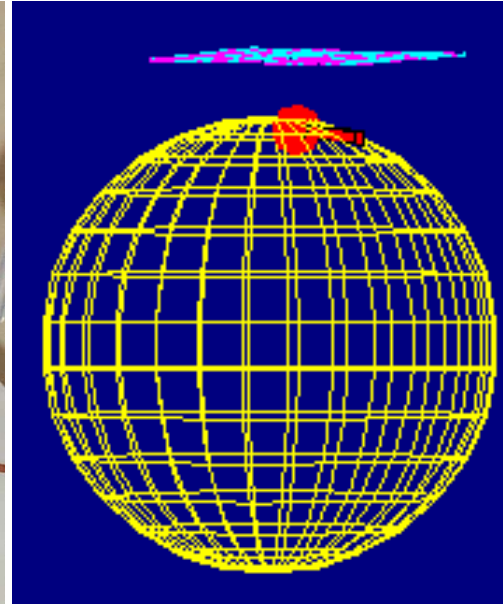
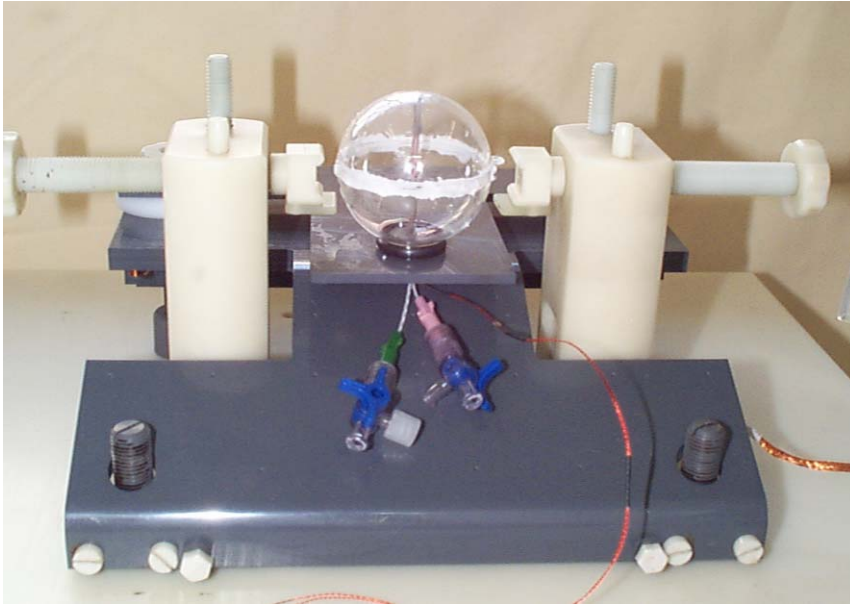


Forward: J.C. de Munck
Inverse: FEM

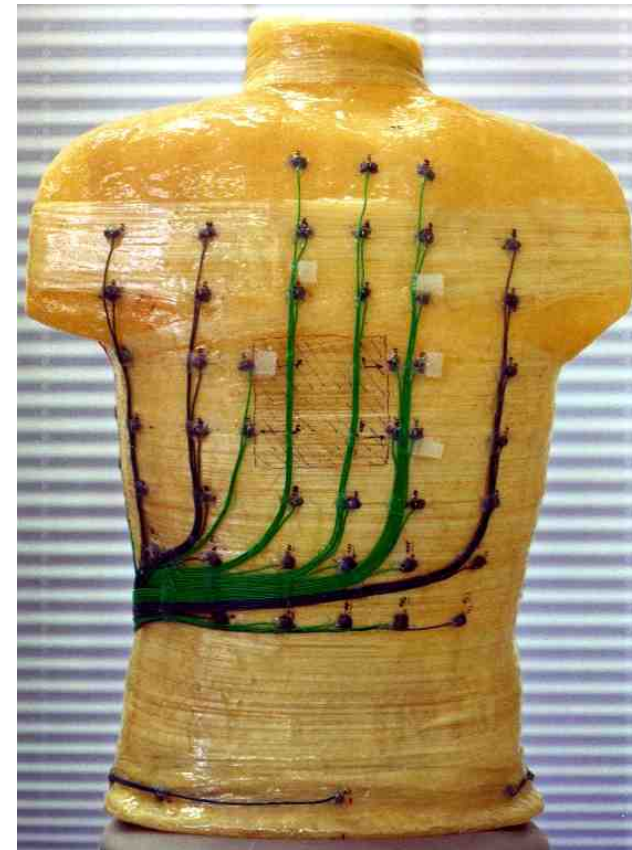
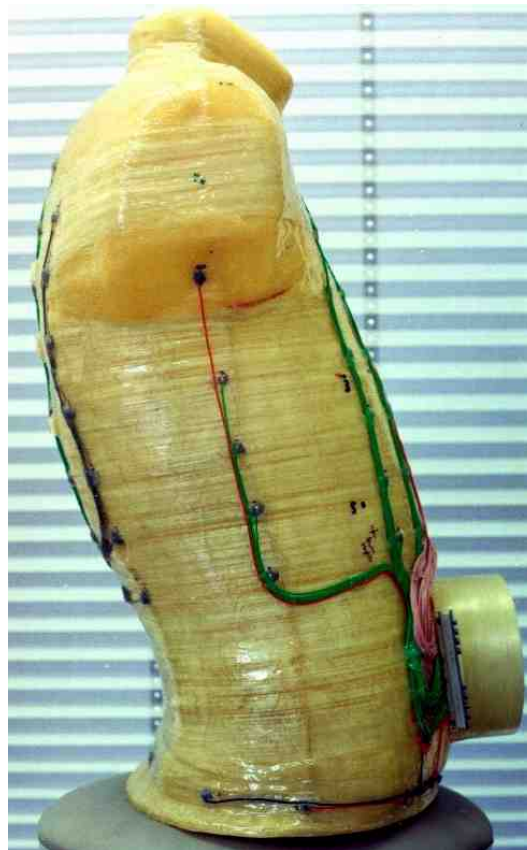
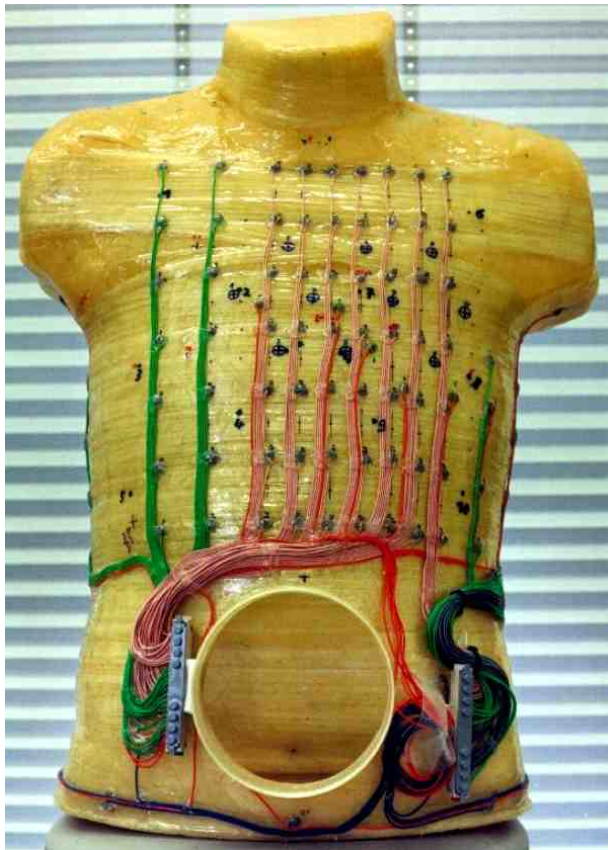
Phantom measurements



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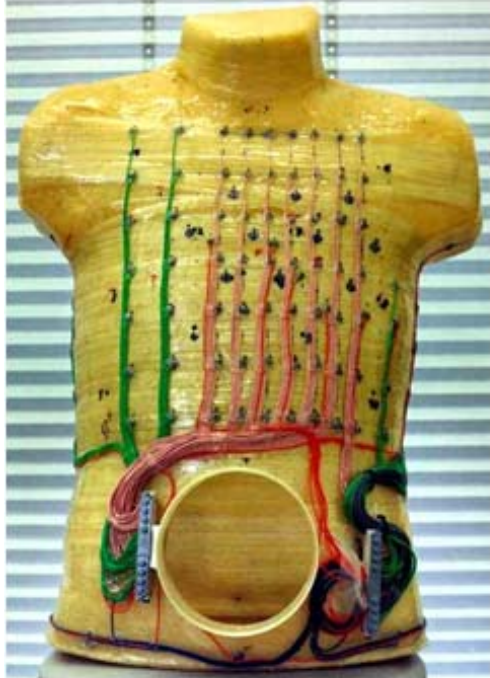


Phantom measurements

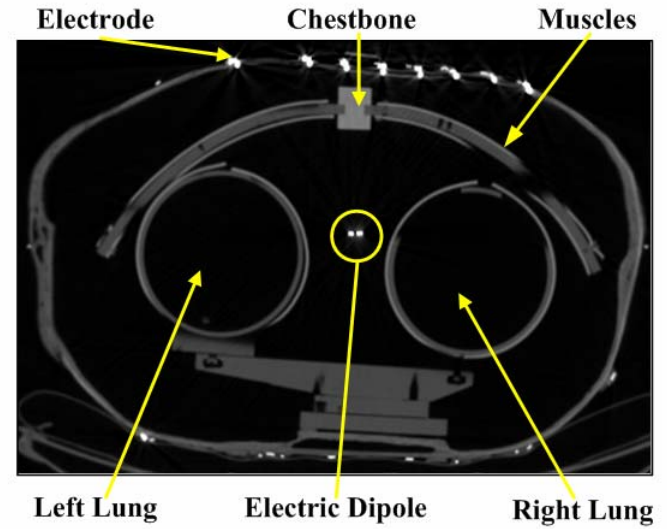


Phantom measurements

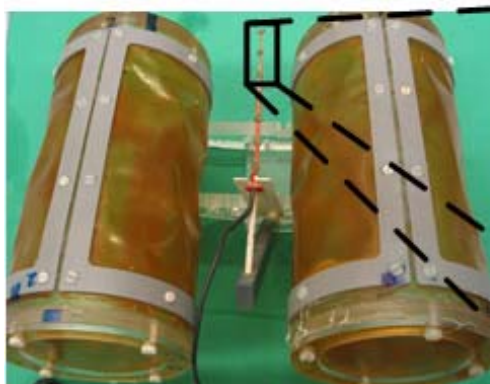
(a)



(b)



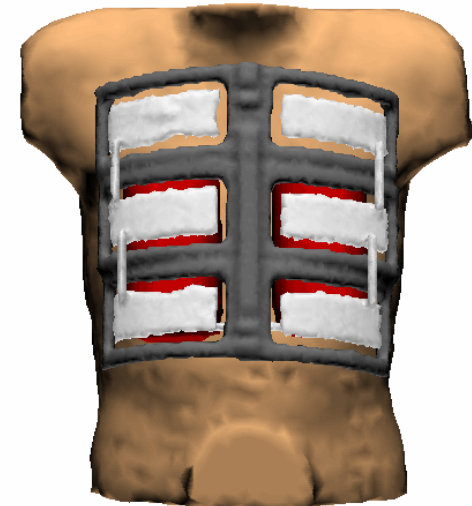
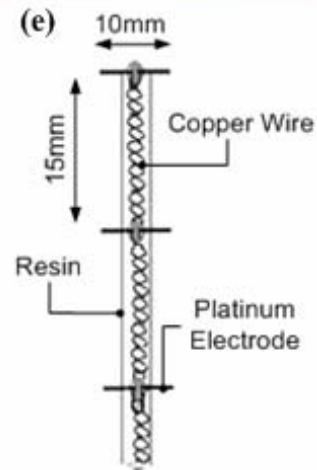
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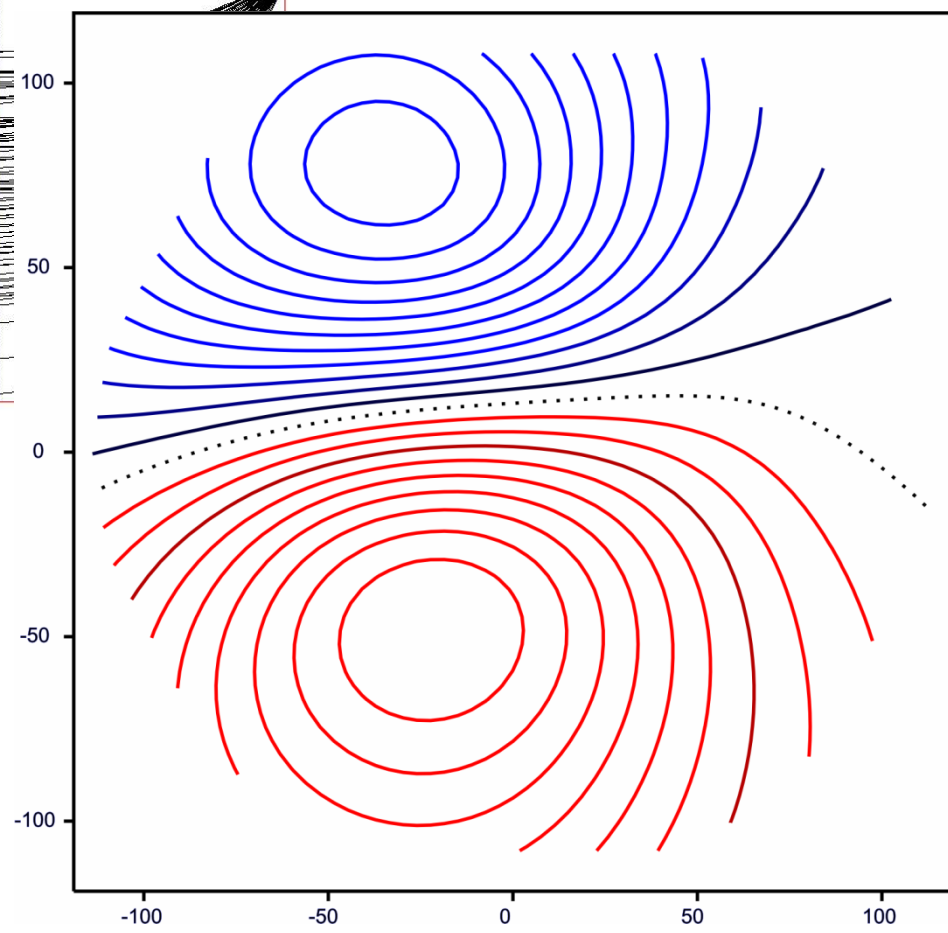
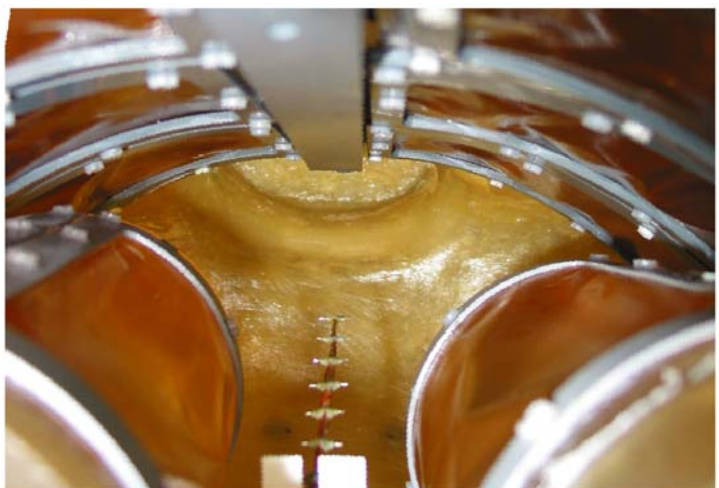
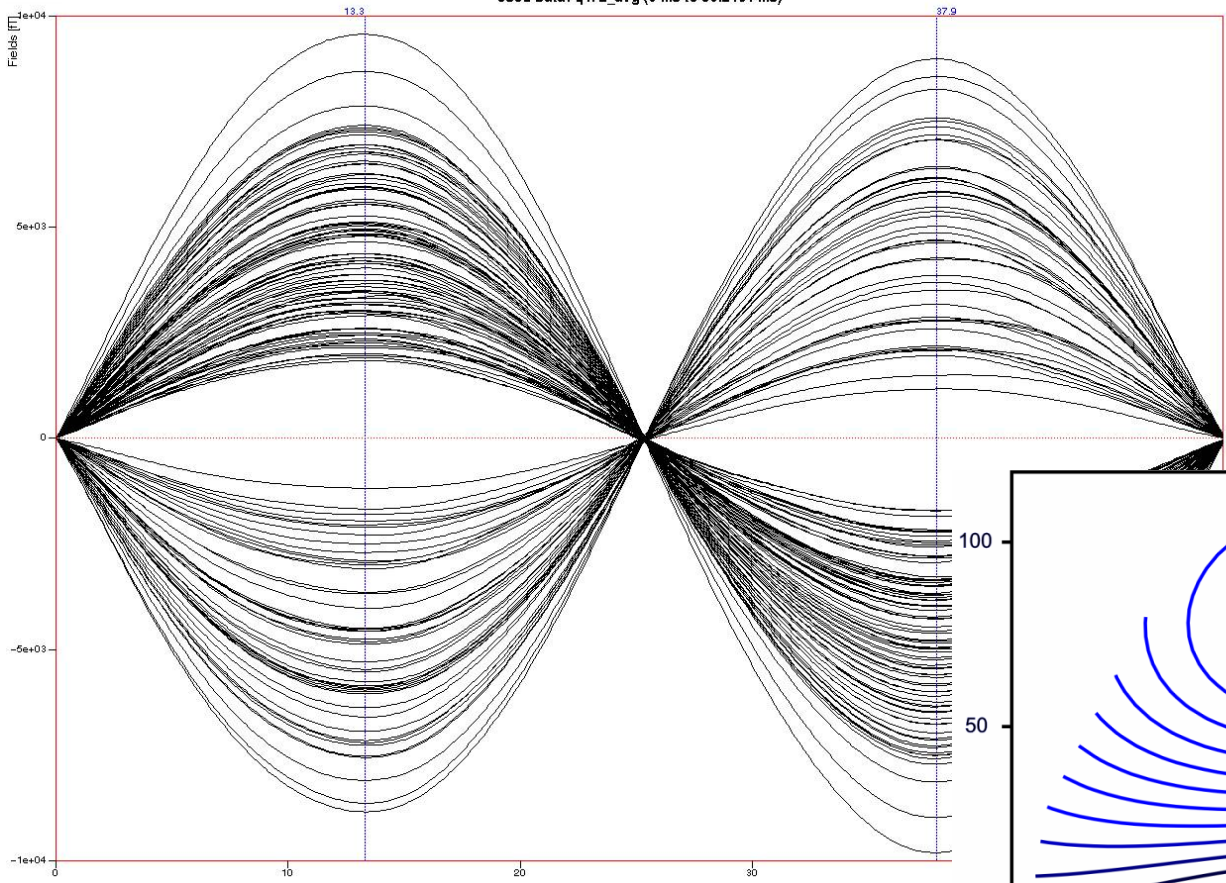


(d)

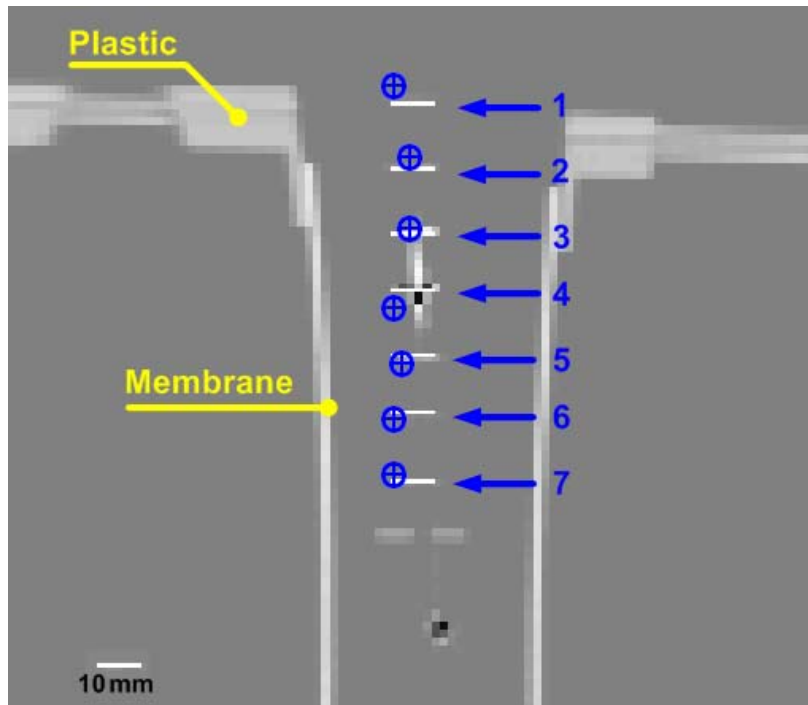


(e)



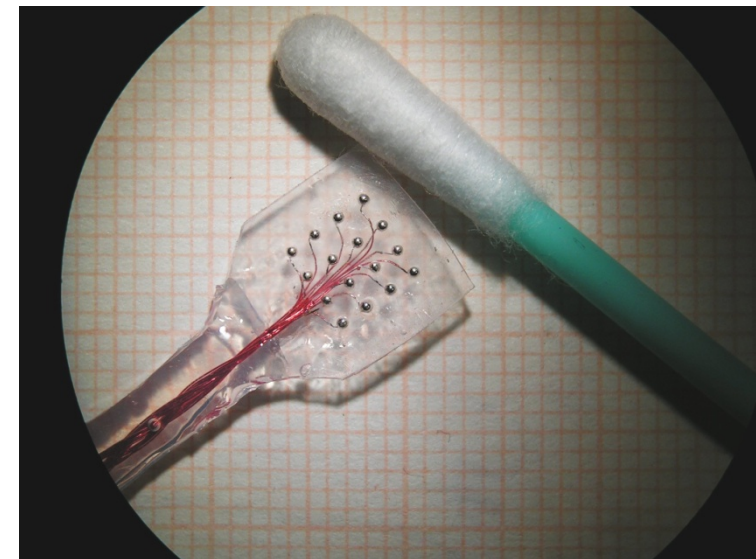


Phantom measurements



Animal measurements

- Combined ECoG and MEG measurements in rabbits
- median nerve / tibial nerve
 - current 0.2 - 0.5 mA
 - Interstimulus interval 503 ms
 - 2048 averages
 - latency
 - 15 - 20 ms (median nerve)
 - 20 - 24 ms (tibial nerve)



Animal measurements



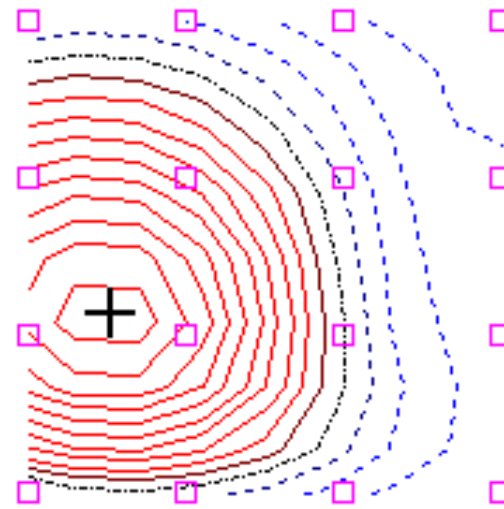
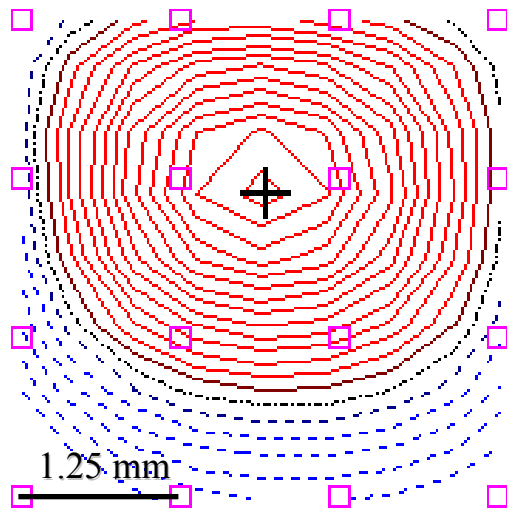
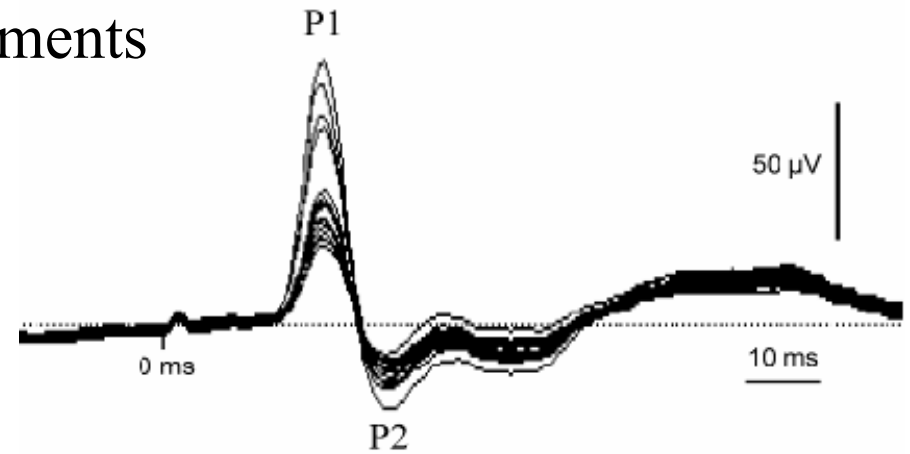
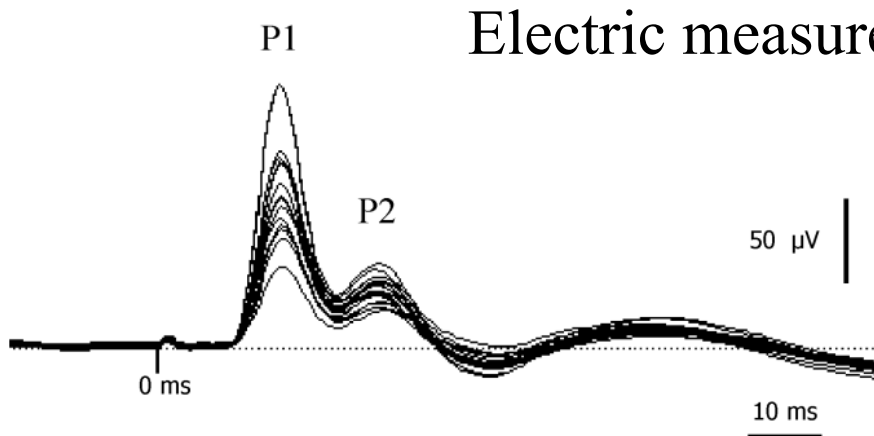
Combined electric measurements (ECoG) with
Compumedics Neuroscan Synamps

Animal measurements

Median nerve

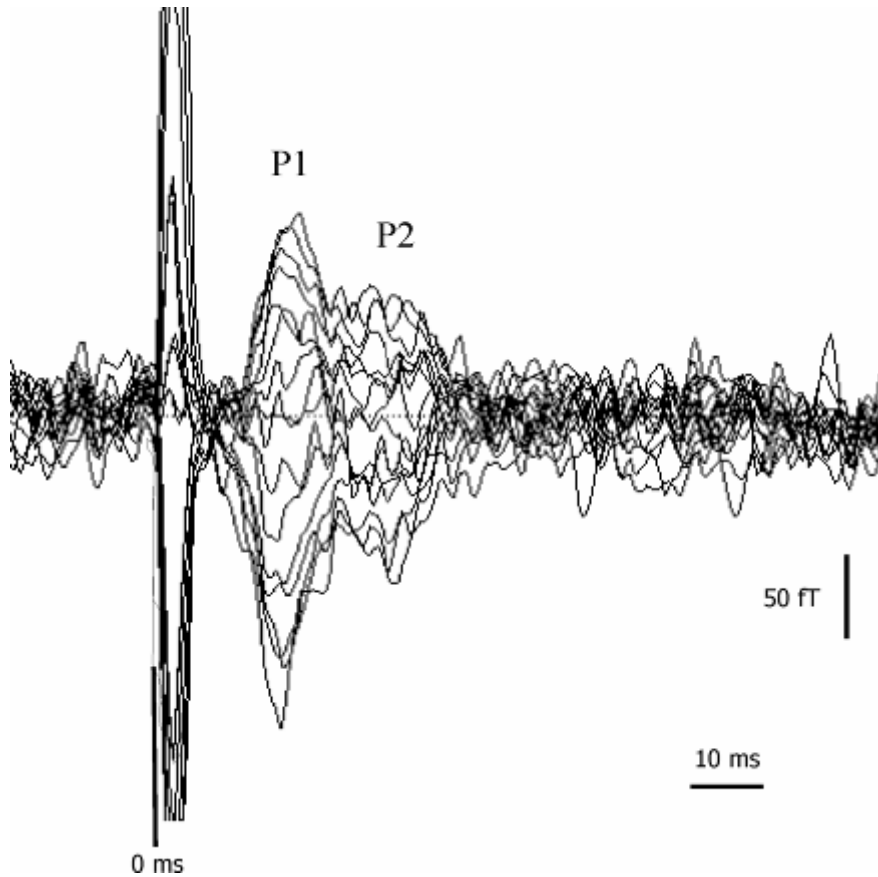
Tibial nerve

Electric measurements

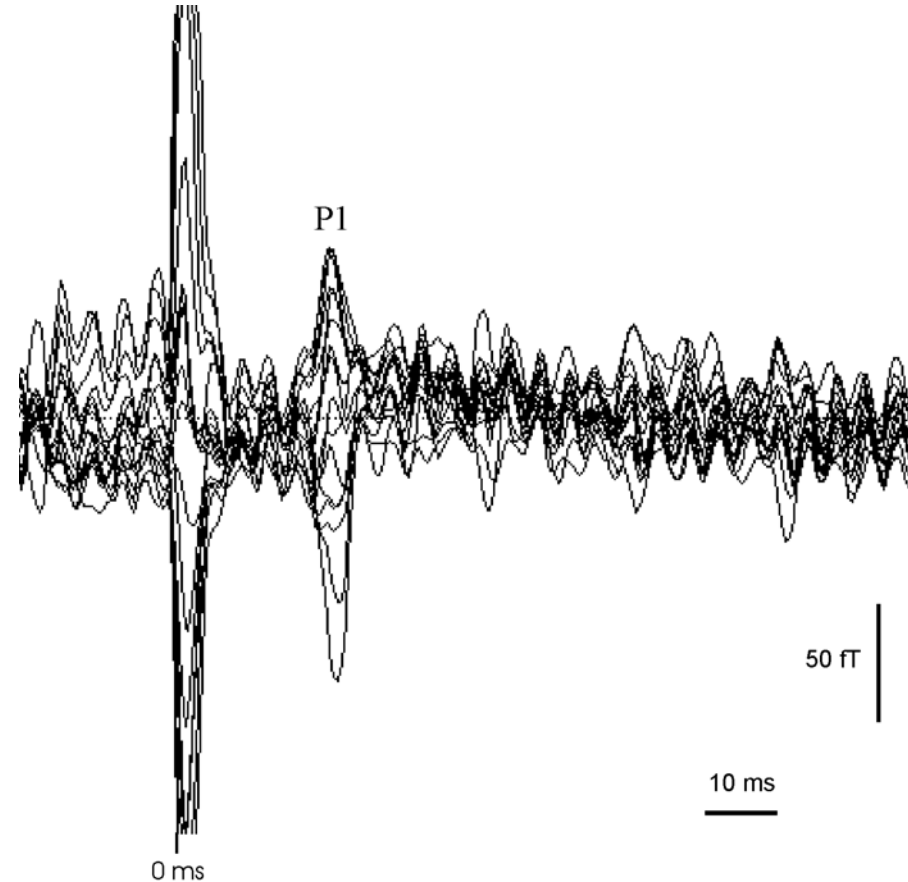


Animal measurements

Median nerve



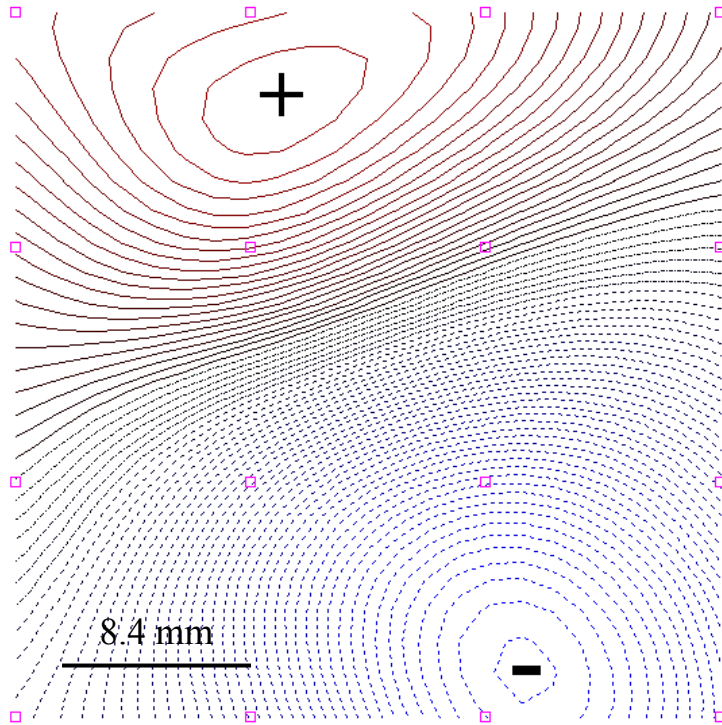
Tibial nerve



Magnetic measurements

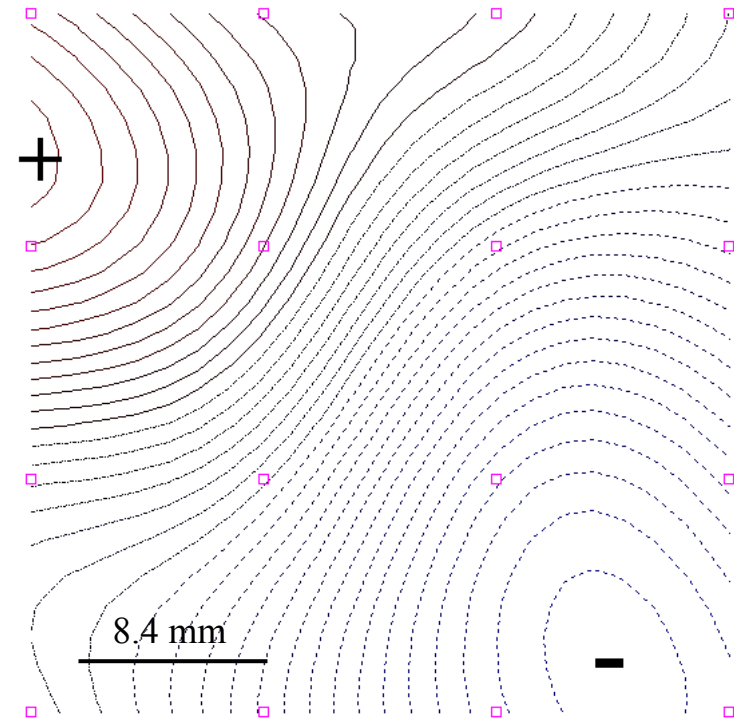
Animal measurements

Median nerve



Time point: 17 ms (P1)
Increment: 5 fT

Tibial nerve



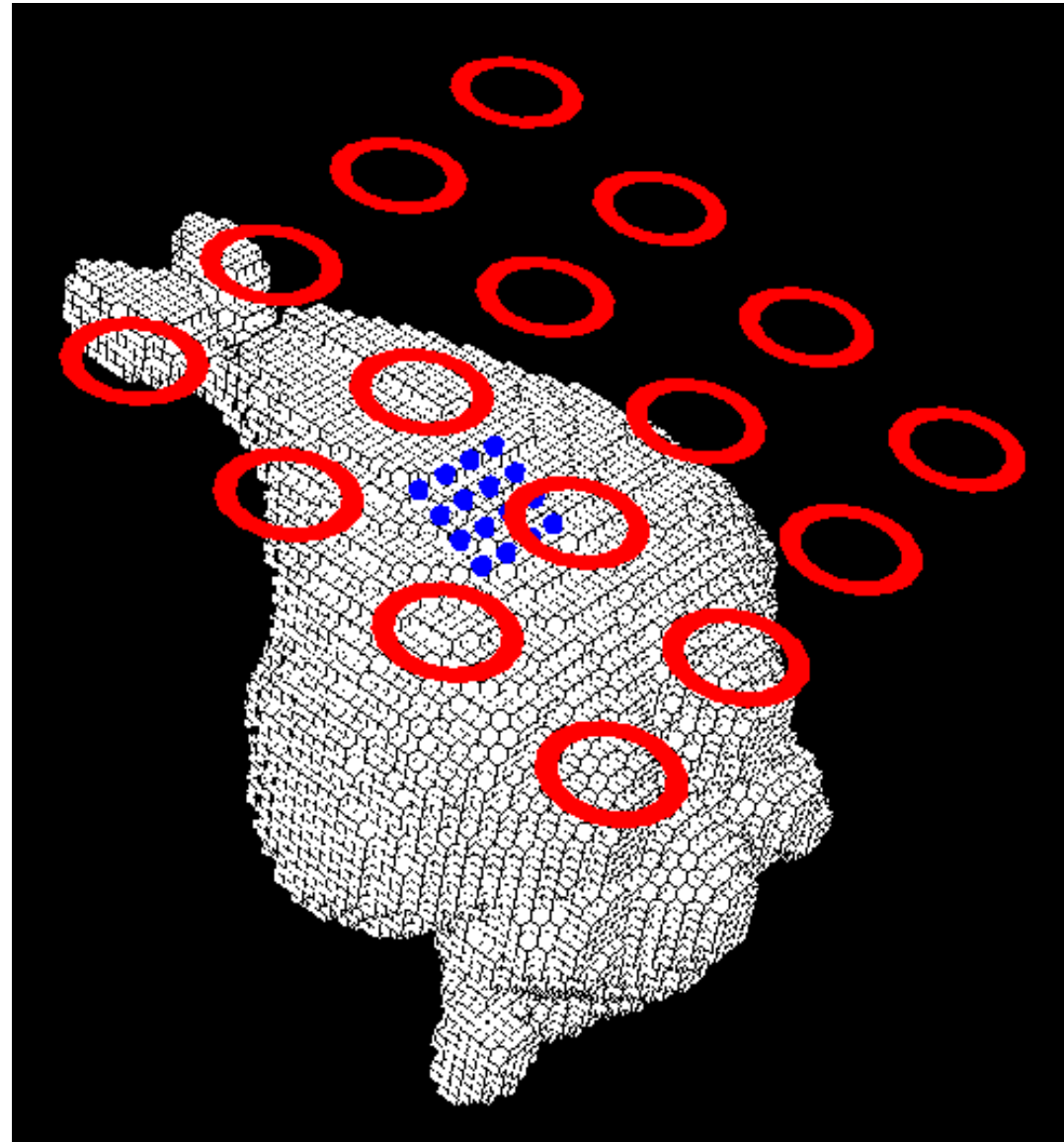
Time point: 21 ms (P1)
Increment: 5 μ V

Magnetic measurements

Animal measurements

Source localization setup

- 16 MEG pick up coils
- 16 electrodes
- One compartment model

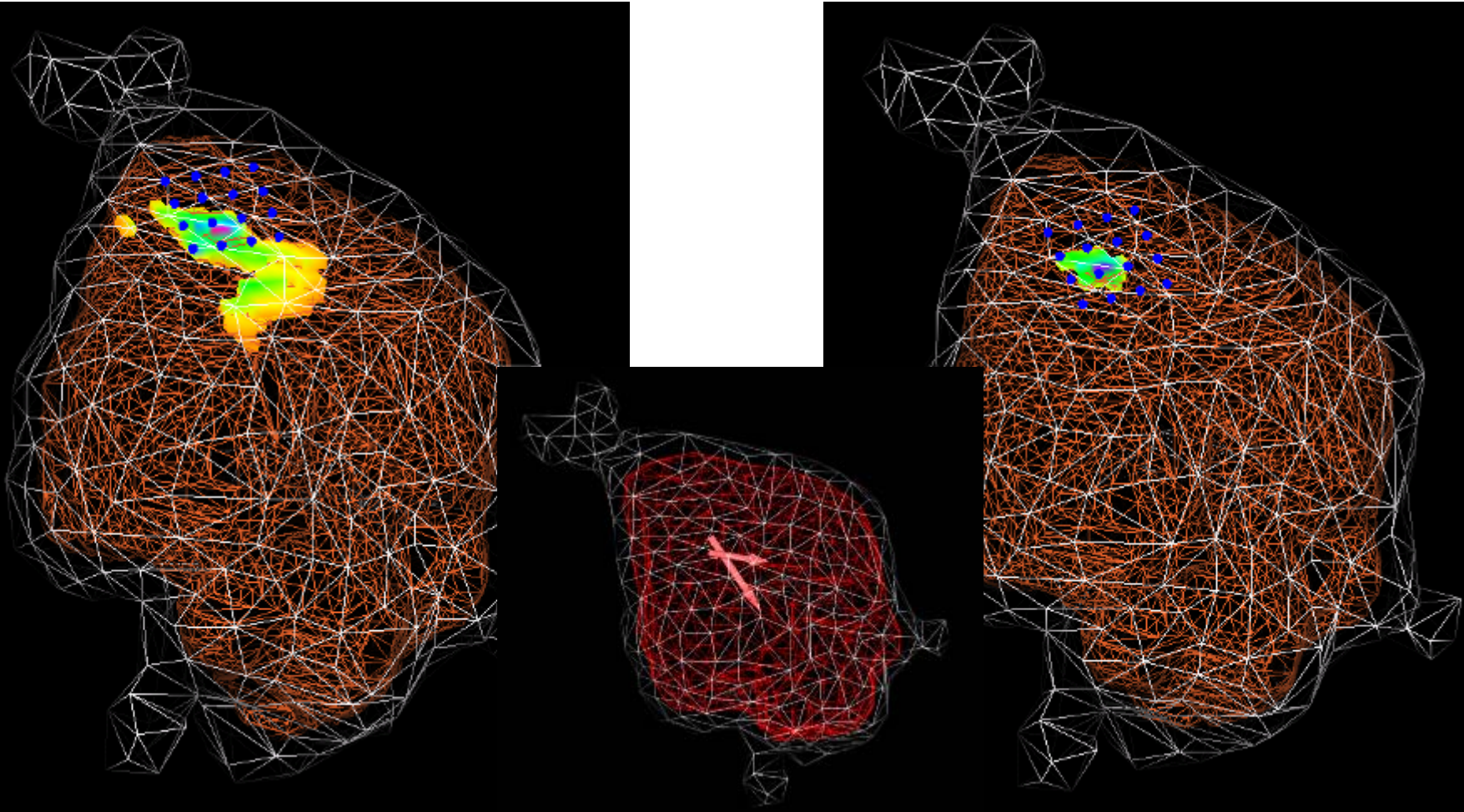


Animal measurements

Comparison median and tibial nerve



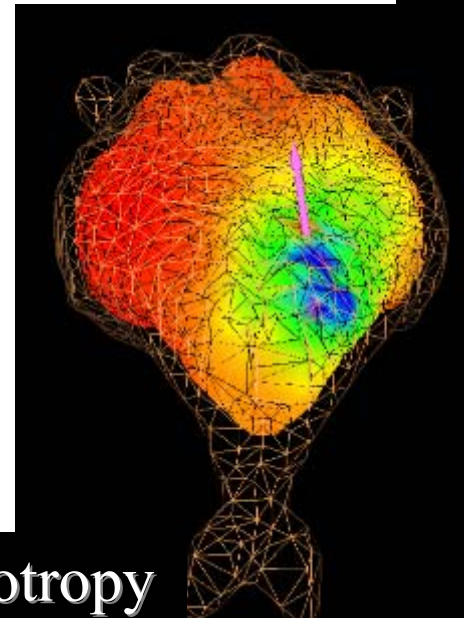
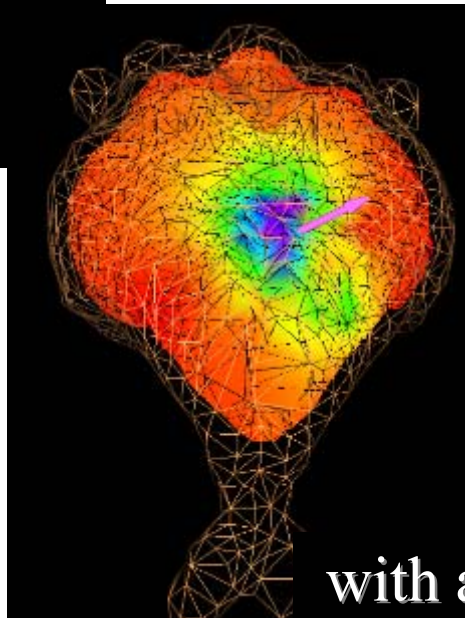
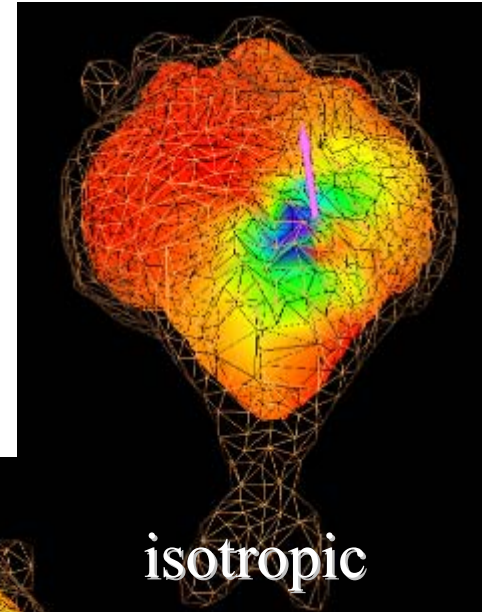
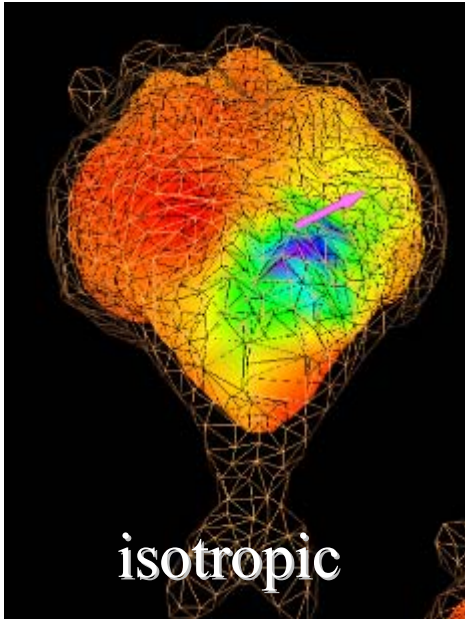
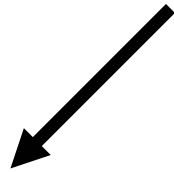
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dip 1 - median nerve: 44.8/46.6/50.5 mm; dip 2 - tibial nerve:
46.2/48.2/50.3); calculated dipole distance 2.1 mm

Influence of anisotropy

median and tibial
nerve



Validation results

- ✓ **Validation in a spherical model successful**
- ✓ **Validation with two stimulus modalities successful**
- ✓ **Validation BEM and FEM successful**
- ✓ **Influence of anisotropy within the procedural limits for median and tibial nerve stimulation**

Thanks to:

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Luca Di Rienzo

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Yoshio Okada

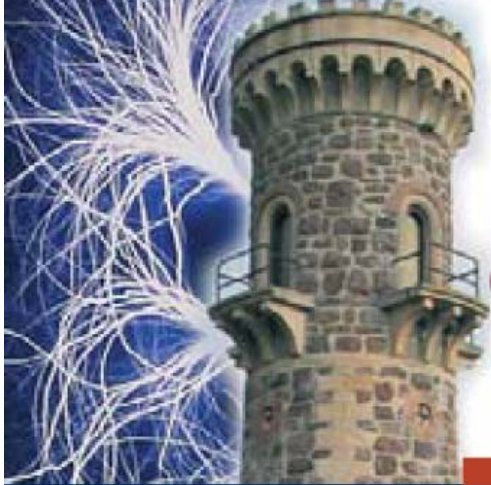
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